

Global Transport of Energetic Particles due to Hole-Clump Production

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Particle Transport Mechanisms of Interest

- **Neoclassical:** Large excursions of resonant particles (banana orbits) + collisional mixing
- **Quasilinear:** Phase-space diffusion over a set of overlapped resonances
- **Convective:** Transport of phase-space holes and clumps by modes with frequency chirping

Important Issue: Individual resonances are narrow. How can they affect every particle in phase space?

Outline

- Quasilinear relaxation near instability threshold
- Phase space holes and clumps (reminder)
- Remnants of frequency sweeping events
- Recurrent production of holes and clumps
- Global redistribution of fast particles

Quasilinear Equations for Bump-on-Tail Instability

- Kinetic equation for fast particles:

$$\frac{\partial F}{\partial t} - \frac{\partial}{\partial V} D \frac{\partial F}{\partial V} = -\nu(F - F_0)$$

- Wave kinetic equation:

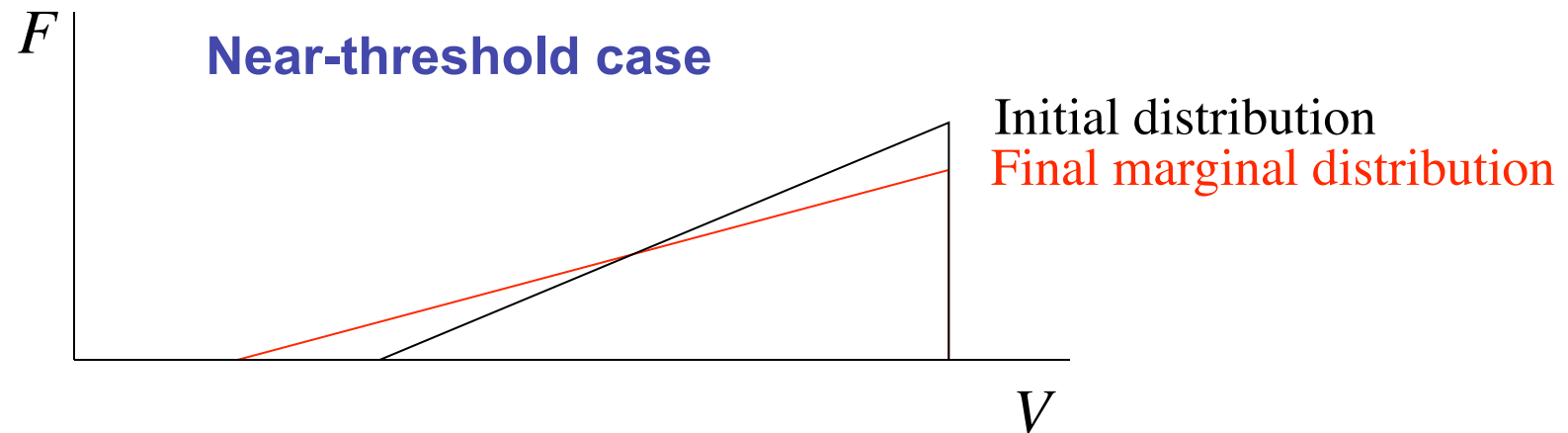
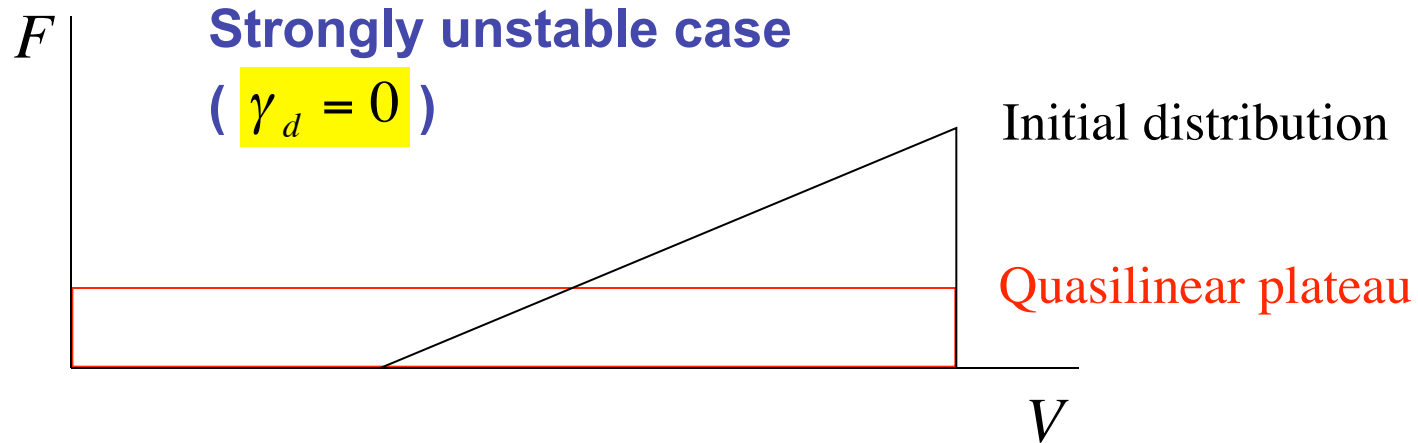
$$\frac{\partial D}{\partial t} = 2(\gamma_L - \gamma_d)D$$

- Instability drive:

$$\gamma_L = \omega_p \frac{\pi}{2n} V^2 \frac{\partial F}{\partial V}$$

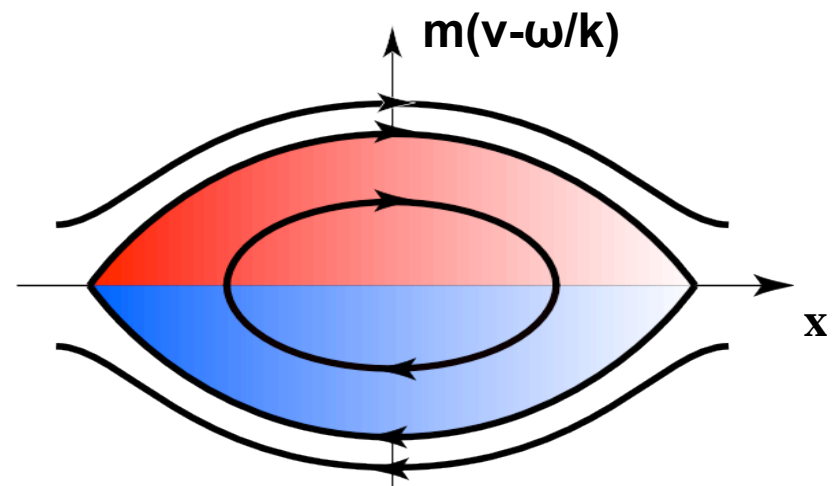
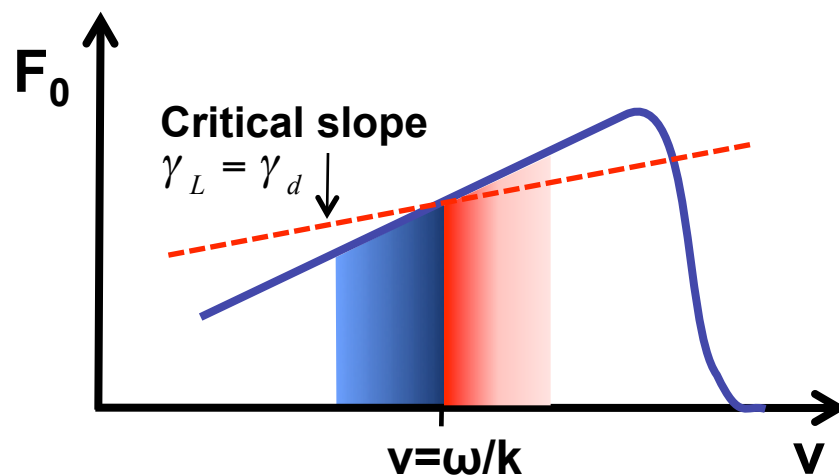
- Background damping: γ_d

Quasilinear Relaxation



Single Mode Theory

- ❑ Unstable initial distribution of energetic particles $F_0(v)$.
- ❑ One linearly unstable mode.
- ❑ Instability drive, γ_L , due to wave-particle resonance ($\omega - kv = 0$).
- ❑ Background dissipation rate, γ_d , determines the critical gradient for the instability.



Single Mode Formalism

$$\frac{\partial F}{\partial t} + u \frac{\partial F}{\partial \zeta} + \frac{ek}{2m} \left[\hat{E}(t) e^{i\zeta} + \text{c.c.} \right] \frac{\partial F}{\partial u}$$
~~$$= \left[v^3 \frac{\partial^2}{\partial u^2} + \alpha^2 \frac{\partial}{\partial u} - \beta \right] (F - F_0)$$~~

$$\frac{\partial \hat{E}}{\partial t} = -4 \frac{\omega}{k^2} \pi e \int f_1 du - \gamma_d \hat{E}$$

$$u \equiv kv - \omega$$

$$\zeta \equiv kx - \omega t$$

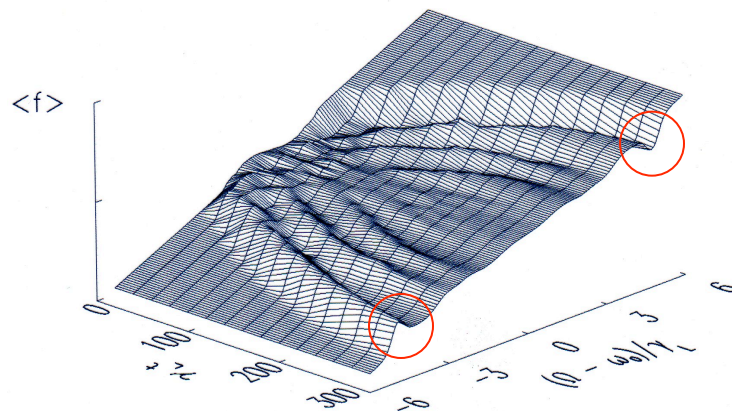
$$F = F_0 + f_0 + \sum_{n=1}^{\infty} \left[f_n \exp(in\zeta) + \text{c.c.} \right]$$

$$E = \frac{1}{2} \left[\hat{E}(t) e^{i\zeta} + \text{c.c.} \right]$$

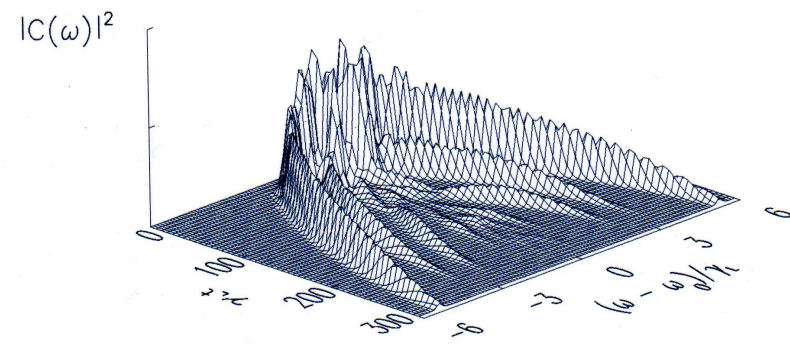
Spontaneous Chirping of Weakly Unstable Mode

- ❑ Simulation of near-threshold bump-on-tail instability (*N. Petviashvili, 1997*) reveals spontaneous formation of coherent phase space structures (clumps and holes) with time-dependent frequencies.
- ❑ The phase space structures seek lower energy states to compensate energy losses due to background dissipation.
- ❑ Clumps move to lower energies and holes move to higher energy regions.

Spatially averaged distribution function



Mode power spectrum

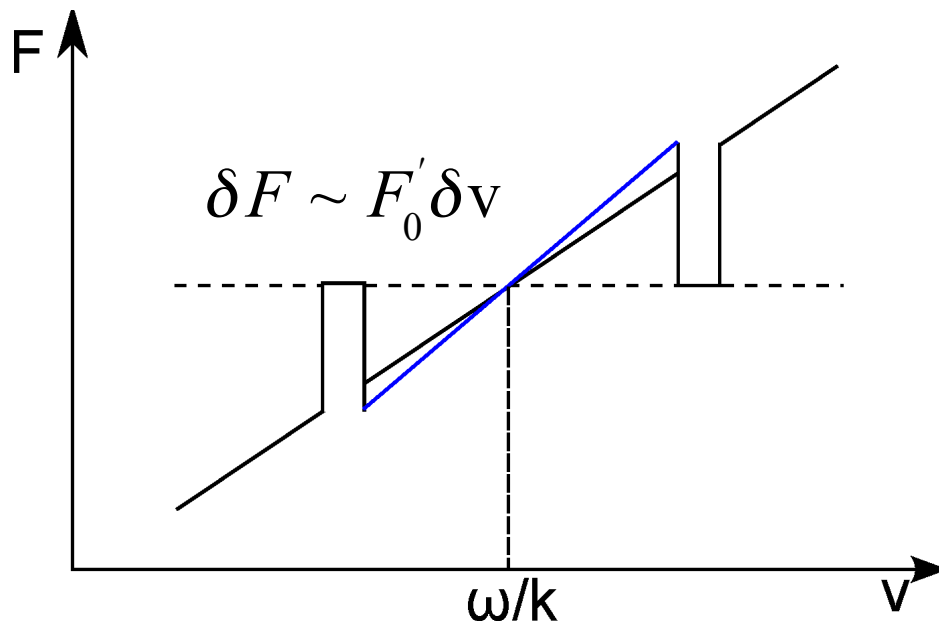


Global Transport Mechanism

- ❑ A single hole or clump affects only a small fraction of the energetic particle phase space.
- ❑ A sweeping event leaves a dent/bulge in the particle distribution function after the wave field decays.
- ❑ Global redistribution requires either many coexisting modes (quasi-linear diffusion scenario) or many sweeping events (this work).
- ❑ Holes and clumps can be generated continuously **without a source** until the distribution changes globally.

Dynamics of Holes and Clumps at Early Times

- Holes/clumps are the original resonant particles
- They move slowly compared to the bounce period



- The wave amplitude is constant:

$$\omega_B = \left(16 / 3\pi^2\right) \gamma_L$$

- Particles cant get inside separatrix.

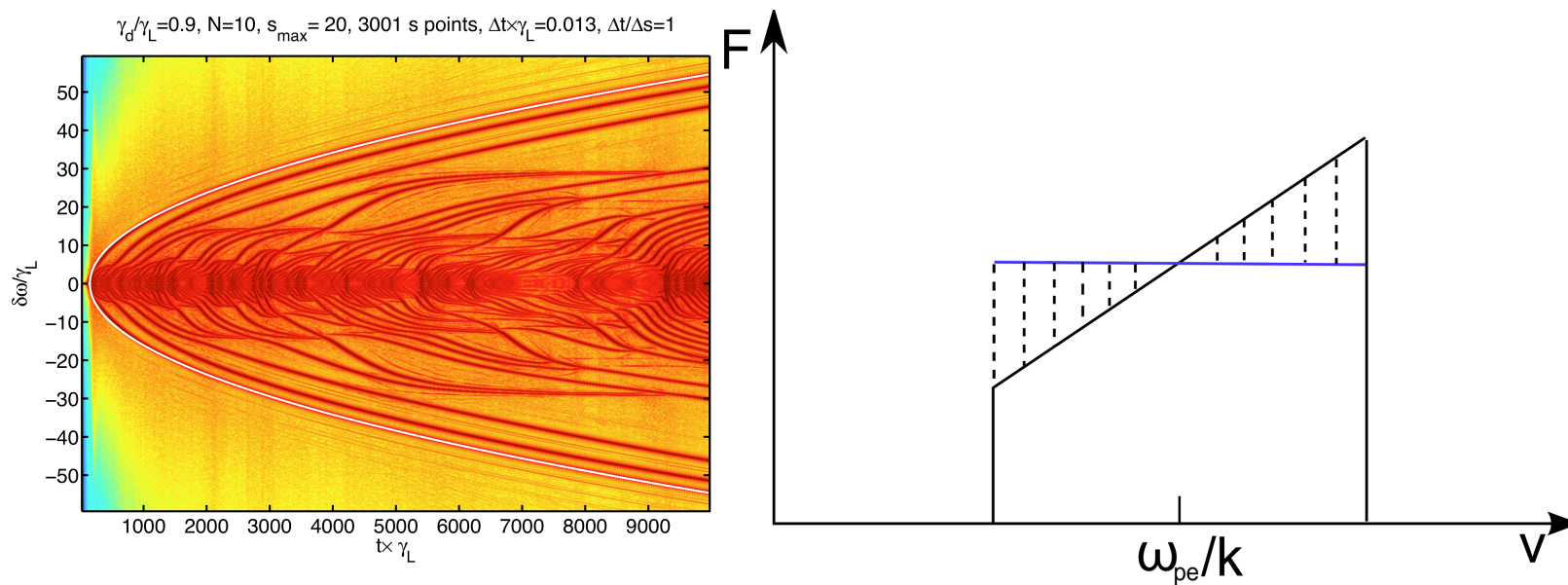
- Hole/clump gets deeper/higher as it moves:

$$\delta\omega = \left(16 / 3\pi^2\right) \gamma_L \sqrt{2\gamma_d t / 3}$$

H.L. Berk, B.N. Breizman, N.V. Petviashvili, Phys. Lett. A 234, 213 (1997)

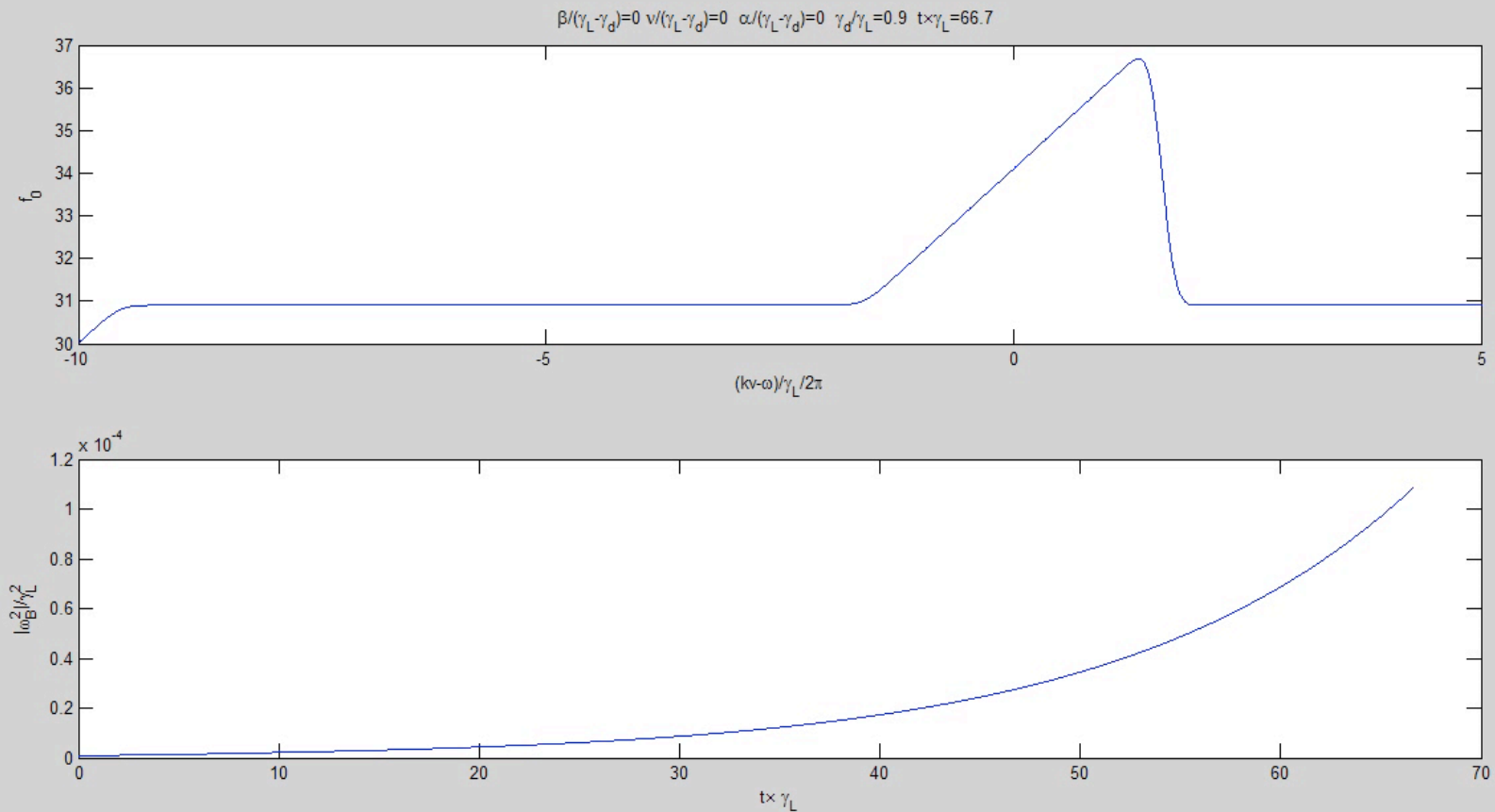
Global Relaxation via Recurrent Sweeping

- ❑ Sweeping modes arise continuously without a source
- ❑ Each mode creates a narrow distortion in the particle distribution
- ❑ The distribution remains perturbed after the mode dies
- ❑ "Stacked up" holes and clumps modify the distribution globally

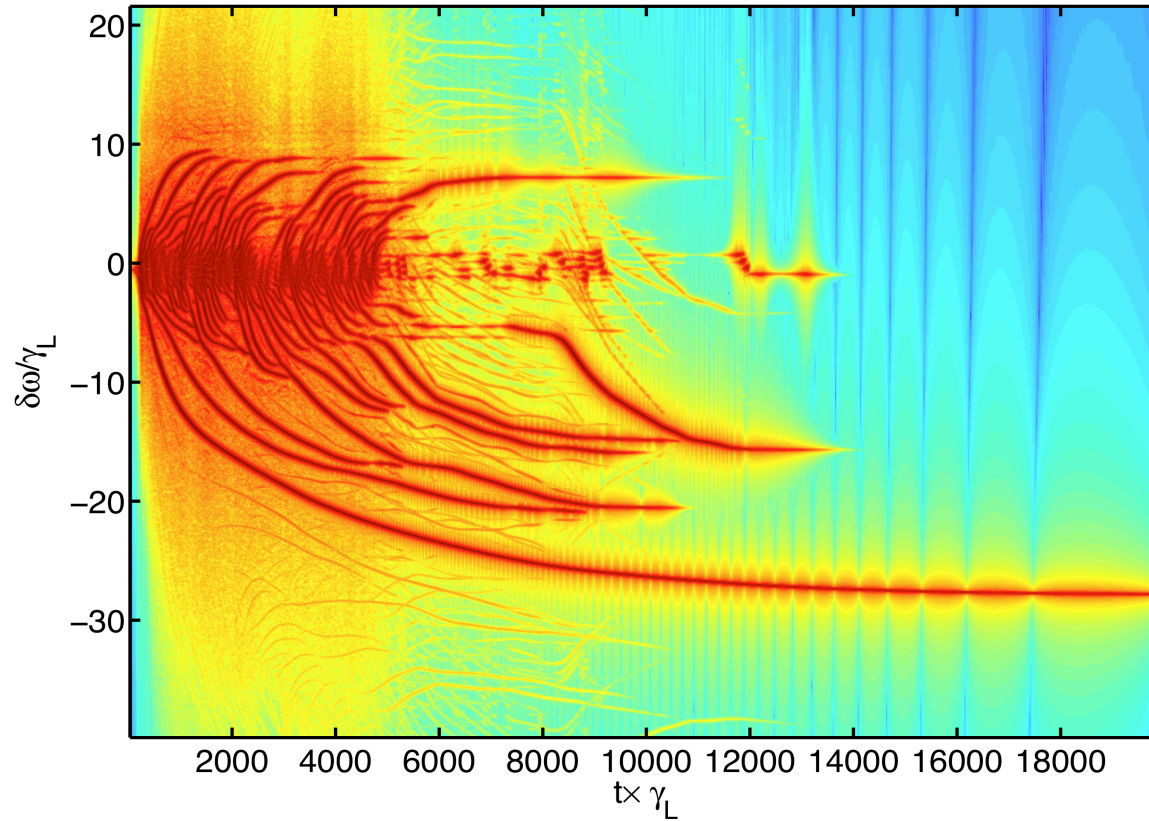


M.K. Lilley, B.N. Breizman, S.E. Sharapov, Phys. Plasmas (2010)

Dynamics of Global Relaxation



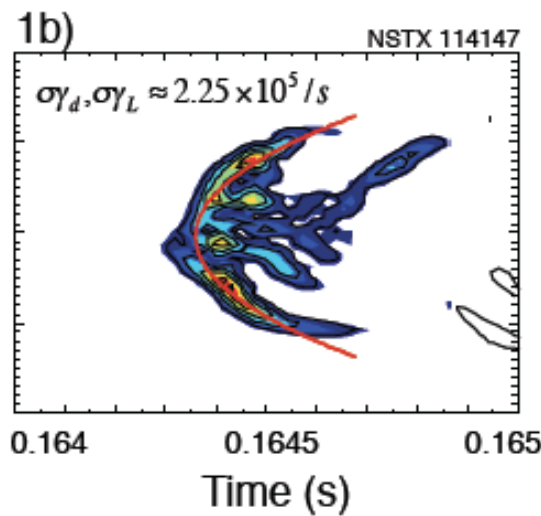
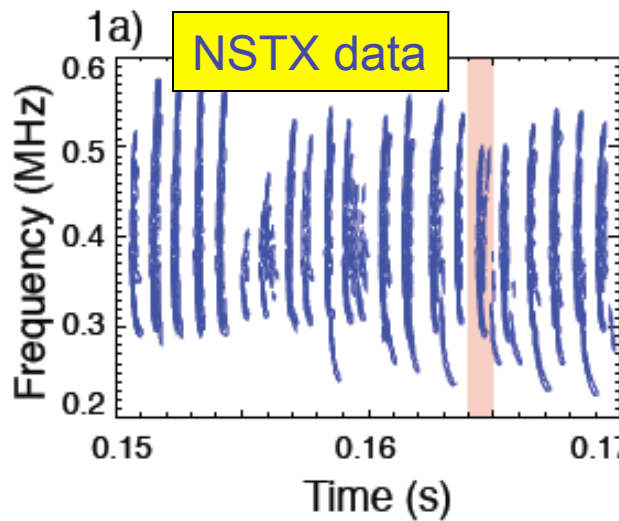
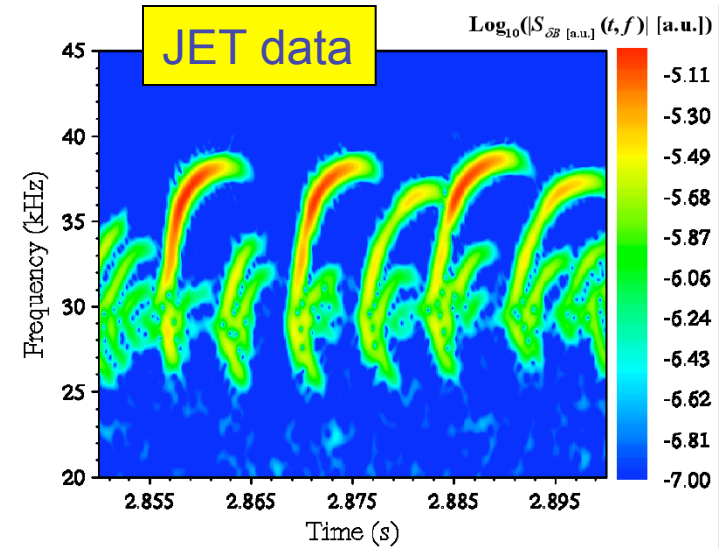
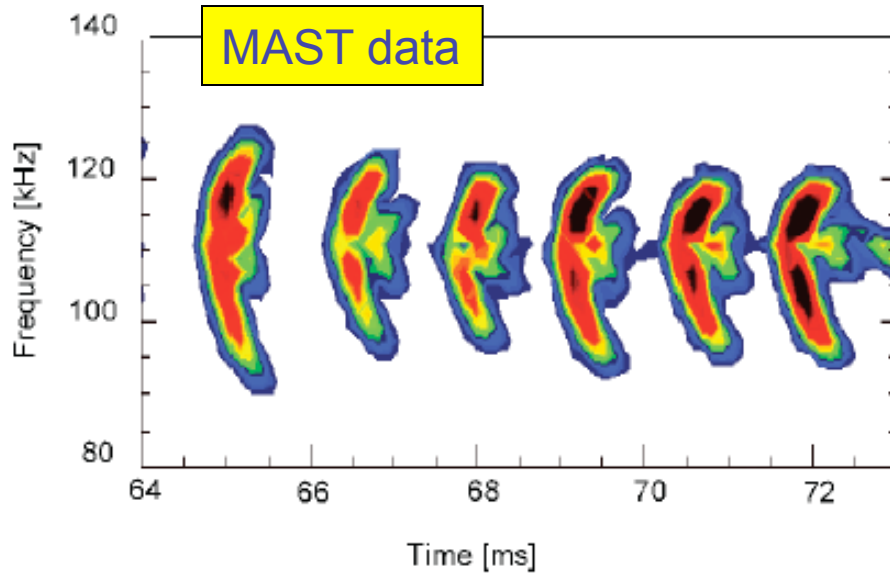
Wave Spectrum During Global Relaxation



Conclusions

- ❑ An isolated resonance can generate recurrent frequency sweeping events that lead to global change in the fast particle distribution.
- ❑ This transport mechanism is convective and it can be more efficient than quasilinear diffusion in the near-threshold regime.

Rapid Frequency Chirping Events

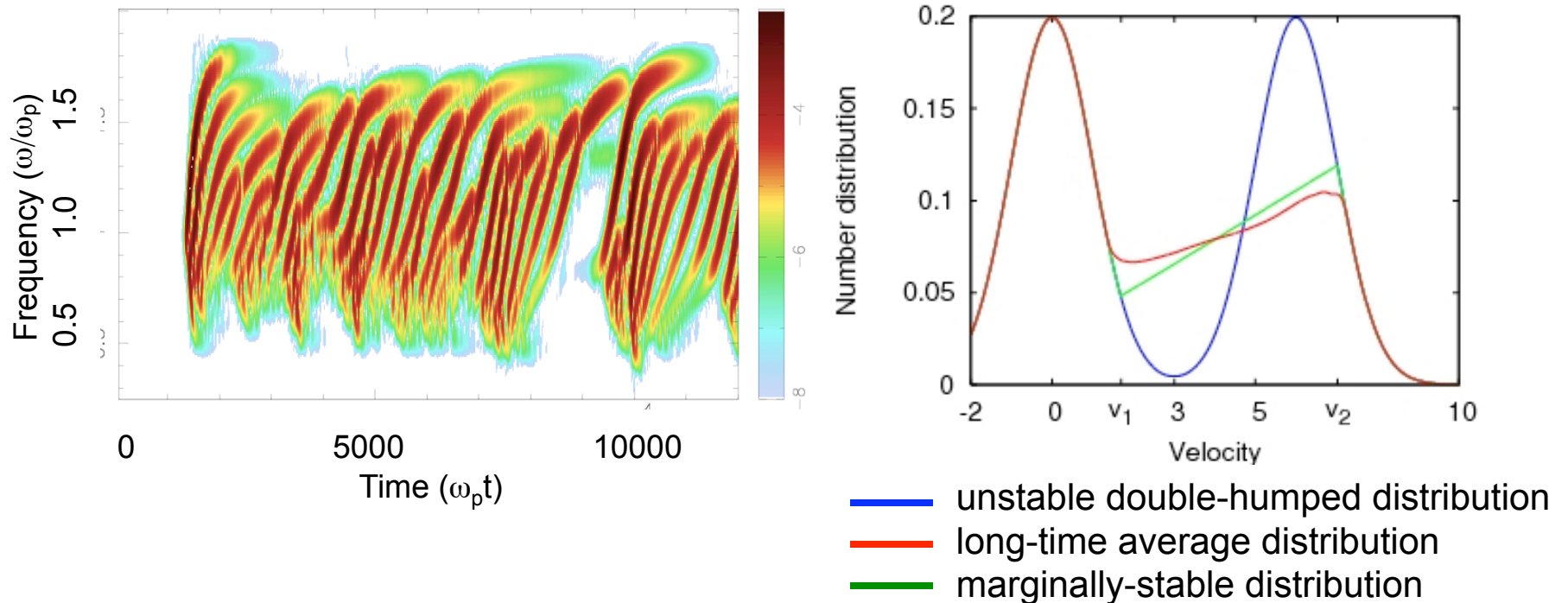


The ms timescale of these events is much shorter than the plasma energy confinement time

Recurrent Chirping Events Maintain Marginally Stable Distribution

Relaxation of unstable double-humped distribution,
with source, sink, and background plasma dissipation.

R.Vann, et al., PRL 99, 025003 (2007)



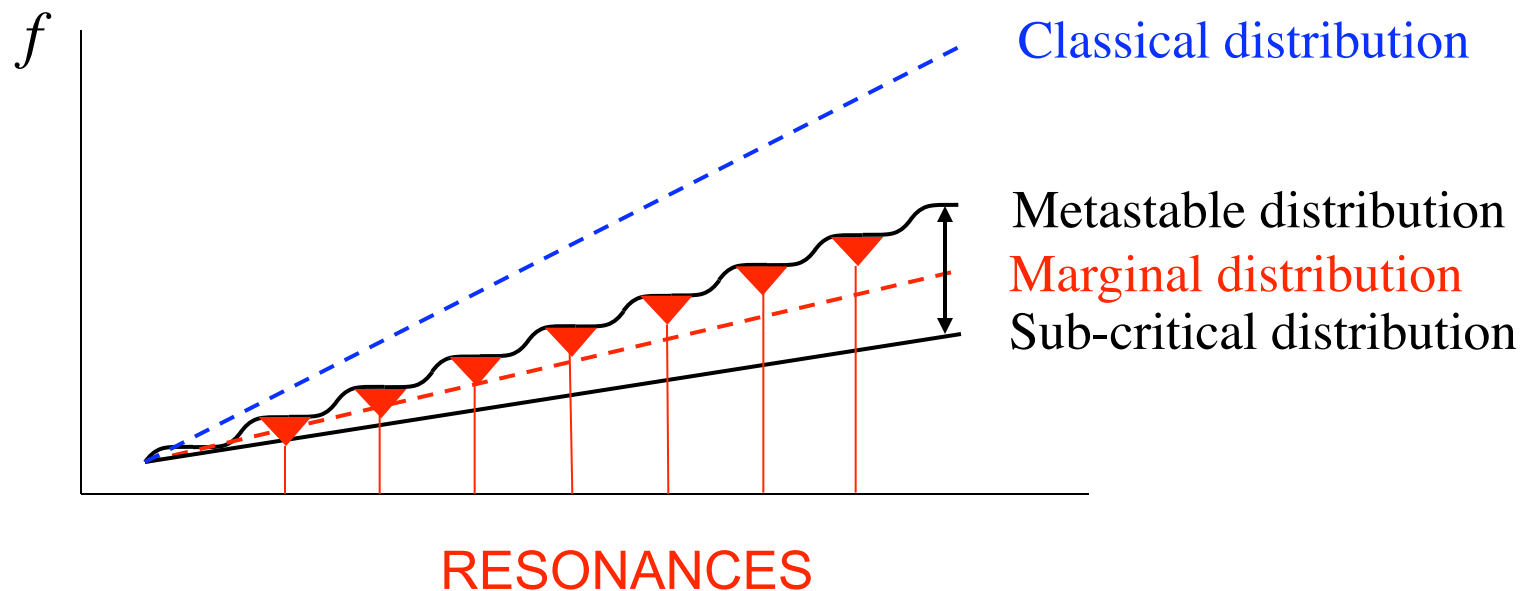
Chirping events facilitate energy exchange between the energetic particles and the bulk plasma.

Intermittent Quasilinear Diffusion

A weak source (with insufficient power to overlap the resonances) is unable to maintain steady quasilinear diffusion



Bursts occur near the marginally stable case



Time Scales and Mode Evolution Phases

γ_L - linear growth rate due to resonant particles

γ_d - background damping rate due to bulk plasma

ω_b - trapped particle bounce frequency

1. Linear near-threshold instability (excitation of a plasma eigenmode)

$$\tau_1 \sim 1/(\gamma_L - \gamma_d) \ll 1/\omega_b$$

2. Explosive nonlinear growth of the mode

Formation of phase-space holes and clumps with trapped particles

Initiation of frequency sweeping

$$\tau_2 \sim 1/\gamma_L \sim 1/\omega_b$$

3. Slow (adiabatic) evolution of phase-space holes and clumps

Significant frequency sweeping

Transition from the bulk plasma eigenmode to a beam mode

$$\tau_3 \gg 1/\gamma_L \sim 1/\omega_b$$